ALLEN[®]

PHYSICAL CHEMISTRY

SOLID STATE

1. Atoms of metals x, y, and z form face-centred cubic (fcc) unit cell of edge length L_x , body-centred cubic (bcc) unit cell of edge length L_y , and simple cubic unit cell of edge length L_z , respectively.

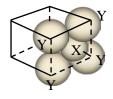
If
$$r_z = \frac{\sqrt{3}}{2}r_y$$
; $r_y = \frac{8}{\sqrt{3}}r_x$; $M_z = \frac{3}{2}M_y$ and $M_z = 3M_x$, then the correct statement (s) is (are)

[Given : M_x , M_y , and M_z are molar masses of metals x, y, and z, respectively.

 r_x , r_y , and r_z are atomic radii of metals x, y, and z, respectively.]

- (A) Packing efficiency of unit cell of x > Packing efficiency of unit cell of y > Packing efficiency of unit cell of z
- (B) $L_y > L_z$
- (C) $L_x > L_y$
- (D) Density of x > Density of y
- Atom X occupies the fcc lattice sites as well as alternate tetrahedral voids of the same lattice. The packing efficiency (in %) of the resultant solid is closest to [JEE(Advanced) 2022]
 (A) 25
 (B) 35
 (C) 55
 (D) 75
- For the given close packed structure of a salt made of cation X and anion Y shown below (ions of only one face are shown for clarity), the packing fraction is approximately [JEE(Advanced) 2021]

$$(packing fraction = \frac{Packing efficiency}{100})$$



(A) 0.74 (B) 0.63

4.

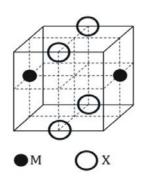
The cubic unit cell structure of a compound containing cation M and anion X is shown below. When compared to the anion, the cation has smaller ionic radius. Choose the correct statement(s).

(C) 0.52

[JEE(Advanced) 2020]

(D) 0.48

[JEE(Advanced) 2023]



- (A) The empirical formula of the compound is MX.
- (B) The cation M and anion X have different coordination geometries.
- (C) The ratio of M-X bond length to the cubic unit cell edge length is 0.866.
- (D) The ratio of the ionic radii of cation M to anion X is 0.414.

- Consider an ionic solid MX with NaCl structure. Construct a new structure (Z) whose unit cell is constructed from the unit cell of MX following the sequential instructions given below. Neglect the charge balance. [JEE(Advanced) 2018]
 - (i) Remove all the anions (X) except the central one
 - (ii) Replace all the face centered cations (M) by anions (X)
 - (iii) Remove all the corner cations (M)
 - (iv) Replace the central anion (X) with cation (M)

The value of $\left(\frac{\text{number of anions}}{\text{number of cations}}\right)$ in Z is_____.

- 6. A crystalline solid of a pure substance has a face-centred cubic structure with a cell edge of 400 pm. If the density of the substance in the crystal is $8g \text{ cm}^{-3}$, then the number of atoms present in 256g of the crystal is $N \times 10^{24}$. The value of N is : [JEE(Advanced) 2017]
- 7. The **CORRECT** statement(s) for cubic close packed (ccp) three dimensional structure is (are)

[JEE(Advanced) 2016]

- (A) The number of the nearest neighbours of an atom present in the topmost layer is 12
- (B) The efficiency of atom packing is 74%
- (C) The number of octahedral and tetrahedral voids per atom are 1 and 2, respectively
- (D) The unit cell edge length is $2\sqrt{2}$ times the radius of the atom
- 8. If the unit cell of a mineral has cubic close packed (ccp) array of oxygen atoms with m fraction of octahedral holes occupied by aluminium ions and n fraction of tetrahedral holes occupied by magnesium ions m and n respectively, are [JEE(Advanced) 2015]
 - (A) $\frac{1}{2}, \frac{1}{8}$ (B) $1, \frac{1}{4}$ (C) $\frac{1}{2}, \frac{1}{2}$ (D) $\frac{1}{4}, \frac{1}{8}$

SOLUTIONS

1. Ans. (A, B, D)

Sol.

Element	Х	Y	Z
Packing	FCC	BCC	Primitive
Edge	L _x	Ly	Lz
Relation between edge length and radius	$L_x = 2\sqrt{2}r_x$	$L_{y} = \frac{4}{\sqrt{3}} r_{y}$	$L_z = 2r_z$
Packing fraction	$\frac{\pi}{3\sqrt{2}}$	$\frac{\sqrt{3}\pi}{8}$	$\frac{\pi}{6}$

Now,
$$\mathbf{r}_{y} = \frac{8}{\sqrt{3}} \mathbf{r}_{x} \& \mathbf{r}_{z} = \frac{\sqrt{3}}{2} \mathbf{r}_{y} = \frac{\sqrt{3}}{2} \times \frac{8}{\sqrt{3}} \mathbf{r}_{x} \Longrightarrow \mathbf{r}_{z} = 4\mathbf{r}_{x}$$

So,
$$L_x = 2 \sqrt{2} r_x$$
, $L_y = \frac{4}{\sqrt{3}} \times \frac{8}{\sqrt{3}} r_x$, $L_z = 8r_x$
 $L_x = 2 \sqrt{2} r_x$, $L_y = \frac{32}{3} r_x$, $L_z = 8r_x$

So,
$$L_y > L_z > L_x$$

Density $\frac{4M_x}{L_x^3}$, $\frac{2 \times M_y}{L_y^3}$

Now,
$$3M_x = \frac{3M_y}{2}$$
 or $M_x \times 2 = M_y$

$$\frac{\text{density}(x)}{\text{density}(y)} = \frac{4M_x}{2M_y} \times \frac{L_y^3}{L_x^3} = \frac{4M_x}{4M_x} \times \frac{\left(\frac{32}{3}\right)^3}{\left(2\sqrt{2}\right)^3}$$

Hence d(x) > d(y)

2. Ans. (B)

Sol. Atom 'X' occupies FCC lattice points as well as alternate tetrahedral voids of the same lattice

$$\Rightarrow \frac{1}{4} \text{th distance of body diagonal}$$

$$= \frac{\sqrt{3}a}{4} = 2r_x$$

$$\Rightarrow a = \frac{8r_x}{\sqrt{3}}$$
Number of atoms of X per unit cell
$$= 4 + 4 = 8$$
(FCC lattice points) (Alternate tetrahedral voids)

3

% packing efficiency =
$$\frac{\text{Volume occupied by X}}{\text{Volume of cubic unit cell}} \times 100$$

= $\frac{8 \times \frac{4}{3} \pi (r_X)^3}{a^3} \times 100 = \frac{8 \times \frac{4}{3} \pi (r_X)^3}{\left(\frac{8r_X}{\sqrt{3}}\right)^3} \times 100$
= $\left(8 \times \frac{4}{3} \times \pi \times \frac{1}{8^3} \times 3\sqrt{3}\right) \times 100 = \frac{\sqrt{3}\pi}{16} \times 100 = 34\%$

Hence, option (B) is the most appropriate option

Sol. Packing fraction (P.F.) =
$$\frac{1 \times \frac{4}{3} \pi r_{-}^{3} + 3 \times \frac{4}{3} \pi r_{+}^{3}}{a^{3}}$$

$$\frac{r_+}{r_-} = 0.414$$
 (square planar void), a = 2r_ r_-

We get,

P.F. =
$$\frac{\frac{4}{3}\pi(r_{-}^{3}+3r_{+}^{3})}{8r_{-}^{3}} = \left[\frac{\pi}{6}(1+3(0.414)^{3})\right] = 0.63$$

4. Ans. (A, C)

Sol. (A)
$$Z_M = 2 \times \frac{1}{2} = 1$$

 $Z_X = 4 \times \frac{1}{4} = 1$

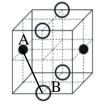
- .:. Empirical formula is MX
- (B) Coordinate numbers of both M and X is 8.
- $(C) \quad \text{Bond length of } M-X \text{ bond}$

= AB =
$$\sqrt{3} \cdot \frac{a}{2} = 0.866$$
ba
(D) $r_{M} : r_{X} = (\sqrt{3} - 1) : 1 = 0.732 : 1.000$

4

Sol.
$$X^{\Theta} \Rightarrow O.V.$$

	$M^+ \Rightarrow FCC$	
	\mathbf{M}^+	\mathbf{X}^{-}
(i)	4	1
(ii)	4–3	3+1
(iii)	4 - 3 - 1	3+1
(iv)	1	3
	$Z = \frac{3}{1} = 3$	



JEE Advanced Chemistry 10 Years Topicwise Questions with Solutions

6. Ans. (2)

Sol. Formula of density = $\frac{Z \times M}{N_A \times a^3}$

For FCC unit cell Z = 4

Edge length $a = 4 \times 10^{-8}$ cm

$$M = \frac{d \times N_A \times a^3}{Z} = \frac{8 \times 6 \times 10^{23} \times 64 \times 10^{-24}}{4} \text{ gm/mol}$$

No. of atoms = $\frac{\text{wt}(\text{gm})}{\text{molar mass}} \times N_{\text{A}} = \frac{256 \times 10 \times 6 \times 10^{23}}{8 \times 6 \times 16} = 2 \times 10^{24}$ (Value of N = 2)

7. Ans. (B, C, D)

- Sol. CCP is ABC ABC type packing
 - (A) In topmost layer, each atom is in contact with 6 atoms in same layer and 3 atoms below this layer.

(B) Packing fraction =
$$\frac{4 \times \frac{4}{3} \pi r^3}{\left(\frac{4r}{\sqrt{2}}\right)^3} = (0.74)$$

(C) Each FCC unit has effective no of atoms = 4

Octahedral void = 4

Tetrahedral void = 8

(D) $4r = a\sqrt{2}$

8. Ans. (A)

Sol. Effective number of $O^{-2} = 4$

Effective number of $Al^{+3} = 4 m$

Effective number of $Mg^{+2} = 8 m$

 \Rightarrow By charge balance 12 m + 16 n = 8

$$3 m + 4 n = 2$$

Possible value of m and n from given equation are

$$m = \frac{1}{2}$$
; $n = \frac{1}{8}$