# **PRACTICE PAPER-2**

## CLASS - XII

## SUBJECT: MATHEMATICS

Time: 3 Hrs. Max. Marks: 80

# General Instructions:

- This question paper contains **FIVE SECTIONS A, B, C, D and E.** Each section is 1. compulsory. However, there are internal choices in some question.
- 2. **SECTION A** has **18 MCQ's** and **02 Assertion-Reason** based questions of **1 mark** each.
- 3. **SECTION B** has 5 Very Short Answer (VSA)-type questions of 2 marks each.
- 4. **SECTION** C has 6 Short Answer (SA)-type questions of 3 marks each.
- 5. **SECTION D** has **4 Long Answer (LA)-type** questions of **5 marks** each.
- SECTION E has 3 source based/case based/passage based/integrated units of 6. **assessment** (4 marks each) with sub parts.

## SECTION – A

The following questions are multiple-choice questions with one correct answer. Each question carries 1 mark.

1.	If A is a non-singu	lar square matrix	of order 3 suc	ch that $A^2 = 3A$ , then	value of  A  is:
	( ) 2	(1) (2)	() 0	(1)	27

- (a) -3
- (b) 3
- (c) 9
- (d) 27
- A line AB in three-dimensional space makes angle 45° and 120° with the positive x-axis and the 2. positive y-axis respectively. If AB makes an acute angle  $\theta$  with the positive z-axis, then  $\theta$  equals:
  - (a) 45°
- (b)  $60^{\circ}$
- (c)  $75^{\circ}$
- (d)  $30^{\circ}$
- Let  $\vec{a} = \hat{i} + \alpha \hat{j} + 3\hat{k}$  and  $\vec{b} = 3\hat{i} \alpha \hat{j} + \hat{k}$ . If the area of the parallelogram whose adjacent sides are 3. represented by the vectors  $\vec{a}$  and  $\vec{b}$  is  $8\sqrt{3}$  square units, then  $\vec{a} \cdot \vec{b}$  is:
  - (a) 3
- (b) 2
- (c) 4
- (d) 1

4. If 
$$A = \begin{bmatrix} 0 & -1 & 2 \\ 2 & -2 & 0 \end{bmatrix}$$
,  $B = \begin{bmatrix} 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix}$  and  $M = AB$ , then  $M^{-1}$  is equal to-

(a) 
$$\begin{bmatrix} 2 & -2 \\ 2 & 1 \end{bmatrix}$$

(b) 
$$\begin{bmatrix} 1/3 & 1/3 \\ -1/3 & 1/6 \end{bmatrix}$$

(c) 
$$\begin{bmatrix} 1/3 & -1/3 \\ 1/3 & 1/6 \end{bmatrix}$$

(a) 
$$\begin{bmatrix} 2 & -2 \\ 2 & 1 \end{bmatrix}$$
 (b)  $\begin{bmatrix} 1/3 & 1/3 \\ -1/3 & 1/6 \end{bmatrix}$  (c)  $\begin{bmatrix} 1/3 & -1/3 \\ 1/3 & 1/6 \end{bmatrix}$  (d)  $\begin{bmatrix} 1/3 & -1/3 \\ -1/3 & 1/6 \end{bmatrix}$ 

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- 5.  $\int_0^{\pi} \cos x \ e^{\sin x} dx \text{ is equal to:}$ 
  - (a) e + 1
- (b) e 1
- (c) 1

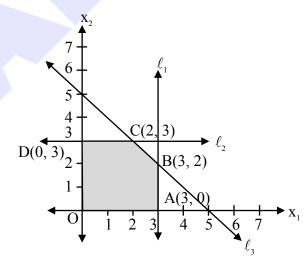
- (d) 0
- **6.** If  $y = \sin(m \sin^{-1} x)$ , then which one of the following equation is true?
  - (a)  $(1-x^2)\frac{d^2y}{dx^2} + x\frac{dy}{dx} + m^2y = 0$
- (b)  $(1-x^2)\frac{d^2y}{dx^2} x\frac{dy}{dx} + m^2y = 0$
- (c)  $(1+x^2)\frac{d^2y}{dx^2} x\frac{dy}{dx} m^2y = 0$
- (d)  $(1+x^2)\frac{d^2y}{dx^2} + x\frac{dy}{dx} m^2x = 0$
- 7. If m and n are the order and degree of the differential equation

$$\left(\frac{d^{2}y}{dx^{2}}\right)^{5} + 4\frac{\left(\frac{d^{2}y}{dx^{2}}\right)^{3}}{\left(\frac{d^{3}y}{dx^{3}}\right)} + \frac{d^{3}y}{dx^{3}} = x^{2} - 1, \text{ then } m + n \text{ is}$$

- (a) 8
- (b) 4
- (c) 6
- (d) 5

- 8. If  $\int \frac{f(x) dx}{\log \sin x} = \log \left[ \log (\sin x) \right]$ , then f(x) is
  - (a) sin x
- (b) cos x
- (c) log sin x
- (d) cot x
- 9. If x = -4 is a root of  $\begin{vmatrix} x & 2 & 3 \\ 1 & x & 1 \\ 3 & 2 & x \end{vmatrix} = 0$ , then the sum of the other two roots is:
  - (a) 4

- (b) -3
- (c) 2
- (d) 5
- 10. The corner points of the feasible region determined by the system of linear inequalities are :



- (a) (0, 0), (-3, 0), (3, 2), (2, 3)
- (b) (3, 0), (3, 2), (2, 3), (0, -3)
- (c) (0, 0), (3, 0), (3, 2), (2, 3), (0, 3)
- (d) None of these

- 11. The solution of differential equation xdy - ydx = 0 represents:
  - (a) a rectangular hyperbola
  - (b) parabola whose vertex is at origin
  - (c) straight line passing through origin
  - (d) a circle whose centre is at origin
- **12.** Two events E and F are independent. If P(E) = 0.3 and  $P(E \cup F) = 0.5$ , then P(E/F) - P(F/E)equals to:
  - (a)  $\frac{2}{7}$
- (b)  $\frac{3}{35}$  (c)  $\frac{1}{70}$  (d)  $\frac{1}{7}$
- **13.** If A is square matrix of order 3 and B = A' such that |A| = -4, then |AB| is equal to :
  - (a) 9
- (b) 12
- (c) 16
- (d) 16
- Let  $\vec{a}$  and  $\vec{b}$  be two non-zero vectors perpendicular to each other and  $|\vec{a}| = |\vec{b}|$ . If  $|\vec{a} \times \vec{b}| = |\vec{a}|$ , **14.** then the angle between the vectors  $(\vec{a} + \vec{b} + (\vec{a} \times \vec{b}))$  and  $\vec{a}$  is:
- (a)  $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$  (b)  $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$  (c)  $\cos^{-1}\left(\frac{1}{\sqrt{2}}\right)$  (d)  $\sin^{-1}\left(\frac{1}{\sqrt{6}}\right)$
- Corner points of the feasible region determined by the system of linear constraints are (0, 3), **15.** (1, 1) and (3, 0). Let Z = px + qy, where p, q > 0. Condition on p and q, so that the minimum of Z occurs at (3,0) and (1, 1) is
  - (a) p = 2q
- (b)  $p = \frac{q}{2}$  (c) p = 3q (d) p = q
- Let I be an identity matrix of order  $2 \times 2$  and  $P = \begin{bmatrix} 2 & -1 \\ 5 & -3 \end{bmatrix}$ . Then the value of K, for which **16.** 
  - $P^6 = KI 8P$ , where  $K \in N$  is.
  - (a) -6
- (b) -5
- (c) 5
- (d) 6
- The area of a triangle formed by vertices O, A and B, where  $\overrightarrow{OA} = \hat{i} + 2\hat{j} + 3\hat{k}$  and **17.**  $\overrightarrow{OB} = -3\hat{i} - 2\hat{j} + \hat{k}$  is:

  - (a)  $3\sqrt{5}$  sq. units (b)  $5\sqrt{5}$  sq. units (c)  $6\sqrt{5}$  sq. units (d) 4 sq. units



$$\left|\frac{|x-1|}{1-x}+a, x>1\right|$$

18. If 
$$f(x) = \begin{cases} a+b & x=1 \text{ is continuous at } x=1, \text{ then the values of 'a' and 'b' are respectively:} \\ \frac{|x-1|}{1-x} + b, x < 1 \end{cases}$$

- (a) 1, 1
- (b) 1, -1
- (c) 2, 3
- (d) None of these

### ASSERTION-REASON BASED QUESTIONS

In the following questions, a statement of **Assertion** (**A**) is followed by a statement of **Reason** (**R**). Choose the correct answer out of the following choices.

- (a) Both A and R are true and R is the correct explanation of A.
- (b) Both A and R are true but R is not the correct explanation of A.
- (c) A is true but R is false.
- (d) A is false but R is true.
- **19. Assertion (A) :** The angle between the lines whose direction cosines are given by the equations  $3\ell + m + 5n = 0$  and  $6mn 2n\ell + 5\ell m = 0$  is  $\cos^{-1}\left(\frac{1}{6}\right)$ .

**Reason (R)**: An angle between two lines is given by 
$$\cos\theta = \left| \frac{a_1 a_2 + b_1 b_2 + c_1 c_2}{\sqrt{a_1^2 + b_1^2 + c_1^2} \sqrt{a_2^2 + b_2^2 + c_2^2}} \right|$$
,

where  $a_1$ ,  $b_1$ ,  $c_1$  and  $a_2$ ,  $b_2$ ,  $c_2$  are direction ratio's of lines.

**20.** Assertion (A): The domain of the function  $\sec^{-1}(2x+1)$  is  $\left(-\infty,\frac{1}{2}\right] \cup \left[\frac{1}{2},\infty\right)$ 

**Reason** (**R**): 
$$\sec^{-1}(-2) = \frac{2\pi}{3}$$

# SECTION – B

This section comprises of very short answer type-questions (VSA) of 2 marks each

21. Let  $\vec{a}, \vec{b}, \vec{c}$  be three vectors such that  $\vec{a} \neq \vec{0}$  and  $\vec{a} \times \vec{b} = 2\vec{a} \times \vec{c}$ ,  $|\vec{a}| = |\vec{c}| = 1$ ,  $|\vec{b}| = 4$  and  $|\vec{b} \times \vec{c}| = \sqrt{15}$ . If  $\vec{b} - 2\vec{c} = \lambda \vec{a}$ , then find the value of  $\lambda$ .

OR

A line makes the same angle  $\theta$ , with each of the x and z-axis. If the angle  $\beta$ , which it makes with y-axis is such that  $\sin^2 \beta = 3 \sin^2 \theta$ , then find the value of  $\cos^2 \theta$ .

- 22. If  $y = x \sin y$  then prove that  $x \frac{dy}{dx} = \frac{y}{1 x \cos y}$ .
- 23. A spherical ball of salt is dissolving in water in such a manner that the rate of decrease of volume at any instant is proportional to the surface. Prove that the radius is decreasing at a constant rate.
- 24. Find the vector of magnitude  $\sqrt{171}$  which is perpendicular to both of the vectors  $\vec{a} = \hat{i} + 2\hat{j} 3\hat{k}$  and  $\vec{b} = 3\hat{i} \hat{j} + 2\hat{k}$ .
- **25.** Find the value of  $\sin^{-1} \left[ \cos \left\{ \sin^{-1} \left( -\frac{\sqrt{3}}{2} \right) \right\} \right]$ ?

OR

Show that the function f: R  $\rightarrow$  {x  $\in$  R : -1 < x < 1} defined by f (x) =  $\frac{x}{1+|x|}$ , x  $\in$  R is one-one.

## SECTION - C

This section comprises of short answer type questions (SA) of 3 marks each

- 26. Evaluate:  $\int_{\pi/6}^{\pi/3} \frac{\sin x + \cos x}{\sqrt{\sin 2x}} dx$
- 27. A and B throw a pair of dice alternately, till one of them gets a total of 10 and wins the game. Find their respective probabilities of winning, if A starts first.
- 28. In a bank, principal increases continuously at the rate of 5% per year. In how many years Rs. 1000 double itself?

OR

Show that the differential equation  $x\cos\left(\frac{y}{x}\right)\frac{dy}{dx} = y\cos\left(\frac{y}{x}\right) + x$  is homogenous and solve it.

**29.** Solve the linear programming problem graphically

Minimize Z = 6x + 21y,

subject to constraints  $x + 2y \le 3$ ,

$$x + 4y \ge 4$$
,  $3x + y \ge 3$ ,

$$x \ge 0, y \ge 0$$

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30. Evaluate: 
$$\int_0^{\pi/2} \frac{\cos x}{1 + \cos x + \sin x} dx$$

OR

Evaluate: 
$$\int_0^{\pi/2} \left| \sin \left( x - \frac{\pi}{4} \right) \right| dx$$

31. Evaluate: 
$$\int \frac{(3x+5)}{(x^3-x^2-x+1)} dx$$

### SECTION – D

This section comprises of long answer-type questions (LA) of 5 marks each

32. If 
$$A = \begin{bmatrix} 3 & 4 & 2 \\ 0 & 2 & -3 \\ 1 & -2 & 6 \end{bmatrix}$$
, find  $A^{-1}$ .

Hence, Solve the following system of equations.

$$3x + 4y + 2z = 8$$

$$2y - 3z = 3$$

$$x - 2y + 6z = -2$$

- 33. Using the method of integration, find the area of the triangular region whose vertices are (2, -2), (4, 3) and (1, 2).
- 34. Find the shortest distance and the vector equation of the line of shortest distance of the lines given by  $\vec{r} = 3\hat{i} + 8\hat{j} + 3\hat{k} + \lambda(3\hat{i} \hat{j} + \hat{k})$

and 
$$\vec{r} = -3\hat{i} - 7\hat{j} + 6\hat{k} + \mu(-3\hat{i} + 2\hat{j} + 4\hat{k})$$

OR

Two insects are crawling along different lines in three-dimension. At time t (min.) the first insect is at point (x, y, z) on the line x = 6 + t, y = 8 - t and z = 3 + t. also at time t (min.) the second insect is at the point (x, y, z) on the line x = 1 + t, y = 2 + t, z = 2t. Assume that the distance are given in inches. How for apart are the insects at t = 6 min.? What is the closest the 2 insect will ever get to each other?

35. Let N denote the set of all natural numbers and R be the relation on  $N \times N$  by  $(a, b) R (c, d) \Leftrightarrow ad(b+c) = bc(a+d)$ . Check whether R is an equivalence relation on  $N \times N$ .

OR

Let  $A = \{x \in Z : 0 \le x \le 12\}$ . Show that  $R = \{(a, b) : a, b \in A, |a - b| \text{ is divisible by } 4\}$  is an equivalence relation. Find the set of all elements related to 1. Also find the equivalence class of 2.

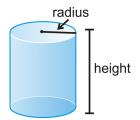


### SECTION – E

(This section comprises of 3 case-study/passage-based questions of 4 marks each with two sub-parts. First two case study questions have three sub-parts (i), (ii), (iii) of marks 1, 1, 2 respectively. The third case study question has two sub-parts of 2 marks each.)

#### **36.** CASE-STUDY: I

A person has manufactured a water tank in the shape of a closed right circular cylinder. The volume of the cylinder is  $\frac{539}{2}$  cubic units. If the height and radius of the cylinder be h and r, then



#### Based on the above information, answer the following questions:

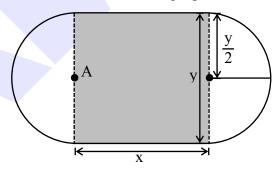
- (i) Find the total surface area function (S) of tank in terms of r.
- (ii) Find the critical points of the functions.
- (iii) Use first order derivative test to find the value of r and h, when surface area of the tank is minimum.

#### OR

(iii) Use second order derivative test to find the value of r and h, when surface area of the tank is minimum.

#### 37. CASE-STUDY: II

An architect designs a building for a multi-national company. The floor consists of a rectangular region with semi-circular ends having a perimeter of 200 m as shown below.



**Design of floor** 

#### Based on the above information answer the following:

- (i) If x and y represents the length and breadth of the rectangular region, then what is the relation between variables x and y.
- (ii) Express the area of the rectangular region A as a function of x.
- (iii) Find the maximum value of area A.

### OR

(iii) The CEO of the multi-national company is interested in maximizing the area of the whole floor including the semi-circular ends, find the maximum area of whole floor.

### 38. CASE-STUDY: III

At the start of a cricket match, a coin is tossed and the team winning the toss has the opportunity to choose to bat or bowl. Such a coin is unbiased with equal probabilities of getting head and tail.



### Based on the above information, answer the following questions:

- (i) If such a coin is tossed 2 times, then find the probability distribution of number of tails
- (ii) Find the conditional probability of getting at least two heads in three tosses of such a coin, if it is know that we get atmost two heads.