

PAPER # 01 - MATHEMATICS

- 1. (a) The probability of an impossible event is 0.
- 2. (c) On a die, there are six numbers 1,2,3,4,5 and 6.
- Total number of possible outcomes = 6 Number on dice which are greater than 4 = 5, 6
- \therefore Favourable number of elementary events = 2
- \therefore Required probability = $\frac{2}{6} = \frac{1}{3}$

3. (b) We have,
$$\sin^2 \theta + \frac{1}{1 + \tan^2 \theta}$$

$$= \sin^2 \theta + \frac{1}{\sec^2 \theta} [\because \sec^2 A = 1 + \tan^2 A]$$

$$= \sin^2 \theta + \cos^2 \theta [\because \sec A = \frac{1}{\cos A}]$$

$$= 1 [\because \sin^2 A + \cos^2 A = 1]$$

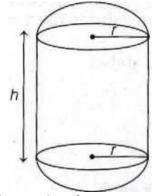
4. (d) We know that area of sector A of radius r and length of arc / is given by

$$A = \frac{1}{2} \ln r$$

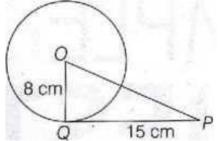
$$\therefore A = \frac{1}{2} \times 3.5 \times 5$$
$$= 8.75 \text{ cm}^2$$

5.

(c)



Total curved surface area = Curved surface area of cylinder + 2 × Curved surface area of hemispheres = 2 π rh + 2 × (2 π r²) = 2 π rh + 4 π r² 6. (b) Given, OQ = 8 cm and PQ = 15 cm.

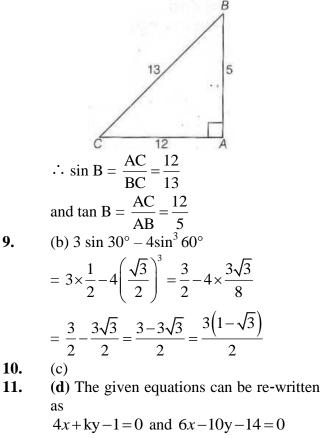


In right angled $\triangle OPQ$, using Pythagoras theorem

$$OP = \sqrt{OQ^{2} + QP^{2}} = \sqrt{8^{2} + 15^{2}}$$

= $\sqrt{64 + 225} = \sqrt{289} = 17 \text{ cm}$
7. (c) $\frac{1}{2}$ [upper limit + lower limit]

8. (c) With reference to $\angle B$, we have Base = AB = 5, perpendicular = AC = 12 and hypotenuse = BC = 13



On comparing with $a_{1x} + b_1y + c_1 = 0$ and

Your Hard Work Leads to Strong Foundation

Page-1



 $a_{2x} + b_2y + c_2 = 0$, we get $a_1 = 4, b_1 = k, c_1 = -1$ $a_2 = 6$, $b_2 = -10$, $c_2 = -14$ and 18 For unique solution, $\frac{\mathbf{a}_1}{\mathbf{a}_2} \neq \frac{\mathbf{b}_1}{\mathbf{o}_2} \qquad \Rightarrow \frac{4}{6} \neq \frac{\mathbf{k}}{-10}$ $\Rightarrow k \neq -\frac{20}{3}$ Thus, given lines have a unique solution for all real values of k, except $-\frac{20}{3}$. 12. (c) Given, AP is 21, 18, 15, ... Here, a = 21 and d = 18 - 21 = -3Let n th term of given AP be -81. 19 Then, $a_n = -81$ \Rightarrow a+(n-1)d = -81[\therefore a_n = a+(n-1)d] ...(i) On putting the values of a and d in Eq. (i), we get $21 + (n - 1) \times (-3) = -81$ $\Rightarrow 21 - 3n + 3 = -81$ $\Rightarrow 24 - 3n = -81$ $\Rightarrow -3n = -81 - 24$ $\therefore n = \frac{-105}{-3} = 35$ 20 Hence, 35th term of given AP is -81. (c) AB = $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ 13. 14. (b) Given, a = 2, $a_{20} = 62$ and n = 20Now, sum of first 20 terms $S_{20} = \frac{20}{2} (2+62) [:: S_n = \frac{n}{2} (a+a_n)]$ $= 10 \times 64 = 640$ (d) HCF (a, b) = 115. LCM (a, b) = ab \therefore HCF (a, b) × LCM (a, b) = 1 × ab = ab (b) Let α and β be the zeroes of $(mx^2 - 6x)$ 16. - 6). Here, a = m, b = -6 and c = -6Given, $\alpha\beta = -3$ $\therefore \frac{c}{a} = -3 \Longrightarrow \frac{-6}{m} = -3 \Longrightarrow m = 2$ (a) Given, $2x^2 - 5x - 3 = 0$ 17. 21 Splitting the middle term, we get $2x^2 - 6x + x - 3 = 0$ \Rightarrow 2x (x - 3) + 1 (x - 3) = 0

$$\Rightarrow (x-3) (2x + 1) = 0$$

$$\Rightarrow x = -\frac{1}{2}, 3$$
3. (c) Given, in $\triangle ABC$ and $\triangle DEF$,

$$\frac{AB}{DE} = \frac{BC}{FD}$$

$$\triangle ABC and \triangle EDF will be similar, if$$

$$\angle B = \angle D [by SAS similarity criterion]$$
0. (c) Assertion sin 60°cos 30° + sin 30°cos

$$60°$$

$$\frac{\sqrt{3}}{2} \left(\frac{\sqrt{3}}{2}\right) + \left(\frac{1}{2}\right) \left(\frac{1}{2}\right) = \frac{3}{4} + \frac{1}{4} = \frac{4}{4} = 1$$

So, Assertion is true.
Reason We know, sin 90° = 1 and cos
90° = 0
So, Reason is false.
Assertion (A) is true but Reason (R) is
false
0. (a) Assertion (A)
Here, $a_1 = 2, b_1 = 3, c_1 = 5$
and $a_2 = 4, b_2 = 6, c_2 = 7 [\because k = 6]$
So, $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \left[\because \frac{2}{4} = \frac{3}{6} \neq \frac{5}{7}\right]$
So, the given system of equations has no
solution (i.e. inconsistent).
So, the Assertion is true.
Reason (R) $a_1x + b_1y + c_1 = 0$
and $a_2x + b_2y + c_2 = 0$
We know, for the system of equations to
be inconsistent,
 $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$
So, both Assertion and Reason are true
and Reason is a correct explanation of
Assertion.
1. Given AB and CD are two parallel
tangents at the point P and Q of a circle
with centre 0.

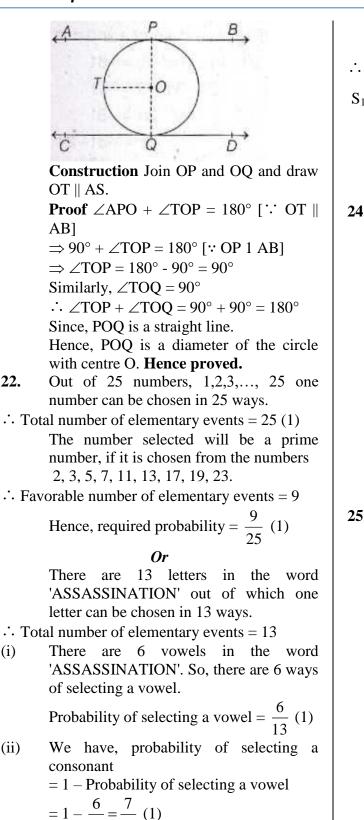
To prove POQ is a diameter of the circle.

22.

(i)

(ii)





$$1 - \frac{6}{13} = \frac{7}{13}$$
 (1)

23. The sequence goes like this 2, 4, 6, 8, ... Here, 4 - 2 = 6 - 4 = 8 - 6 = 2So, it is an AP with first term, a = 2,

common difference. d = 4 - 2 = 2and total number of terms, n = 15 (1) Sum of first 15 even natural numbers $S_{15} = \frac{n}{2} [2a + (n-1)d] = \frac{15}{2} [2 \times 2 + (15-1)2]$ [: S,, = $\frac{n}{2}$ {2a + (n - 1)d}] $=\frac{15}{2}[4+28]=\frac{15}{2}\times 32=240(1)$ Since, x = 2 is a root of the equation 24. $2x^2 + kx - 6 = 0$ $\therefore 2 \times 2^2 + 2k - 6 = 0$ $\Rightarrow 8 + 2k - 6 = 0$ $\Rightarrow 2k + 2 = 0 \Rightarrow k = -1$ (1) On putting k = -1 in the equation $2x^2 +$ kx - 6 = 0, we get $2x^2 - x - 6 = 0 \Longrightarrow 2x^2 - 4x + 3x - 6 = 0$ $\Rightarrow 2x(x - 2) + 3(x - 2) = 0 \Rightarrow (x - 2)(2x + 3)(x - 2)(x - 3)(x - 3)(x - 2)(x - 3)(x - 2)(x - 3)(x - 2)(x - 3)(x - 2)(x - 3)(x -$ (3) = 0 \Rightarrow x - 2 = 0 or 2x + 3 = 0 \Rightarrow x = 2 or $-\frac{3}{2}$ Hence, the other root is $-\frac{3}{2}$. (1) LHS = $\cot A + \tan A = \frac{\cos A}{\sin A} + \frac{\sin A}{\cos A}$ 25. $\left[\because \cot \theta = \frac{\cos \theta}{\sin \theta}, \tan \theta = \frac{\sin \theta}{\cos \theta}\right]$ $=\frac{\cos^2 A + \sin^2 A}{\sin A \cdot \cos A} = \frac{1}{\cos A \cdot \sin A}$ $\left[\because \sin^2 \theta + \cos^2 \theta = 1 \right] (1)$ $=\frac{1}{\sin A}\cdot\frac{1}{\cos A}=\operatorname{cosec} A \sec A$ $\left[\because \operatorname{cosec} \theta = \frac{1}{\sin \theta} \text{ and } \sec \theta = \frac{1}{\cos \theta} \right]$ RHS Hence proved. (1) 0r We have, $\cos^2 30^\circ + \sin^2 45^\circ - \frac{1}{3} \tan^2 60^\circ$ $=\left(\frac{\sqrt{3}}{2}\right)^{2} + \left(\frac{1}{\sqrt{2}}\right)^{2} - \frac{1}{3}\left(\sqrt{3}\right)^{2}$ (1)



$$\begin{bmatrix} \because \cos 30^\circ = \frac{\sqrt{3}}{2} \sin 45^\circ = \frac{1}{\sqrt{2}} \text{ and } \tan 60^\circ = \sqrt{3} \end{bmatrix}$$

$$= \frac{3}{4} + \frac{1}{2} - \frac{3}{3} = \frac{3+2}{4} - 1 = \frac{5}{4} - 1 = \frac{5-4}{4} = \frac{1}{4} (1)$$
26. Given in figure, two chords AS and CD intersect each other at point P. To prove (i) $\Delta APC \sim \Delta DPB$
(ii) $\Delta P \sim \Delta DPB$
(ii) $\Delta P \sim ad DPB$,
 $\angle \Delta PC = \angle DPB$ [vertically opposite angles] and $\angle CAP = \angle BDP$ [vertically opposite angles] and $\angle CAP = \angle BDP$ [so find the same segment]
 $\therefore \Delta APC \sim \Delta DPB$ [by AA similarity criterion] (1)
(ii) We have, $\Delta APC \sim \Delta DPB$ [proved in part (i)]
 $\therefore \frac{AP}{DP} = \frac{CP}{BP} (1)$
[\because if two triangles are similar, then the ratio of their corresponding sides is equal]
 $\therefore AP \cdot BP = CP \cdot DP$ or $AP - PB = CP - DP$ hence proved. (1)
27. Given, a circle is inscribed in the triangle, whose sides are BC = 8cm, AC = 10 cm and AS = 12 cm.
Let $AD = AF = x$, $BD = BE = y$ and $CE = CF = z$
[\because the length of two tangents drawn from an external point to a circle are equal]
We have, $AB = 12$
 $\Rightarrow AD + DB = 12 \Rightarrow x + y = 12 ...(i)$
 $AC = 10 \Rightarrow AF + FC = 10$
 $\Rightarrow x + z - 10 ...(ii)$ and $BC = 8$
 $\Rightarrow CE + EB = 8 \Rightarrow z + y = 8$
 $..(iii)(1)$
On adding Eqs. (i), (ii) and (iii), we get $2(x + y + z) = 12 + 10 + 8$
 $\Rightarrow x + y + z = \frac{30}{2} = 15 ...(iv)$
On putting $x + y = 12$ from Eq. (i) in Eq. (iv), we get $12 + z = 15$
 $\Rightarrow z = 3$

On putting z + y = 8 from Eq. (iii) in Eq, (iv), we get x + 8 = 15 $\Rightarrow x = 7$ (1) On putting x + z = 10 from Eq, (ii) in Eq. (iv), we get 10 + y = 15 $\Rightarrow y = 5$ Hence, AD = 7 cm, BE = 5 cm and CF = 3cm (1)

28. LHS =
$$\frac{\sin A + \cos A}{\sin A - \cos A} + \frac{\sin A - \cos A}{\sin A + \cos A}$$

= $\frac{(\sin A + \cos A)^2 + (\sin A - \cos A)^2}{(\sin A - \cos A)(\sin A + \cos A)}$ (1)
[$\sin^2 A + 2\sin A \cos A + \cos^2 A + \frac{\sin^2 A - 2\sin A \cos A + \cos^2 A}{\sin^2 A - \cos^2 A}$
[$\because (a \pm b)^2 = a^2 + b^2 \pm 2ab$] (1)
= $\frac{2\sin^2 A + 2\cos^2 A}{\sin^2 A - \cos^2 A} = \frac{2(\sin^2 A + \cos^2 A)}{\sin^2 A - \cos^2 A}$
= $\frac{2}{\sin^2 A - \cos^2 A}$ [$\because \sin^2 \theta + \cos^2 \theta = 1$]
= RHS Hence proved. (1)
Or
LHS = $\frac{\sin \theta - \cos \theta + 1}{\sin \theta + \cos \theta - 1} = \frac{\tan \theta - 1 + \sec \theta}{\tan \theta + 1 - \sec \theta}$
[dividing numerator and denominator by $\cos \theta$]
= $\frac{(\tan \theta + \sec \theta) - 1}{(\tan \theta - \sec \theta) + 1}$
[$\tan \theta - \sec \theta$] -1][$\tan \theta - \sec \theta$]
[multiplying and dividing by ($\tan \theta - \sec \theta$]
[$\tan \theta - \sec \theta + 1$][$\tan \theta - \sec \theta$]
[$\tan \theta - \sec \theta + 1$][$\tan \theta - \sec \theta$]
[$(\tan \theta - \sec \theta + 1)(\tan \theta - \sec \theta)$] (1)
= $\frac{(\tan^2 \theta - \sec^2 \theta) - (\tan \theta - \sec \theta)}{(\tan \theta - \sec \theta + 1)(\tan \theta - \sec \theta)}$
[$\because (a - b) (a + b) = a^2 - b^2$]
= $\frac{-1 - \tan \theta + \sec \theta}{(\tan \theta - \sec \theta + 1)(\tan \theta - \sec \theta)}$
[$\because \tan^2 A - \sec^2 A = -1$](1)

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Page-4



$$= \frac{-(\tan \theta - \sec \theta + 1)}{(\tan \theta - \sec \theta + 1)(\tan \theta - \sec \theta)}$$
$$= \frac{-1}{\tan \theta - \sec \theta}$$
$$= \frac{1}{\sec \theta - \tan \theta} = \text{RHS Hence proved. (1)}$$

29. Let A_1 and A_2 be the areas of sectors OAB and OCD respectively. Then, $A_1 =$ Area of a sector of angle 30° in a circle of radius 7 cm

$$\Rightarrow A_1 = \left\{ \frac{30}{360} \times \frac{22}{7} \times 7^2 \right\} \text{ cm}^2$$

$$\left[\text{Using: } A = \frac{\theta}{360} \times \pi r^2 \right]$$

$$\Rightarrow A_1 = 77/6 \text{ cm}^2$$

 A_2 = Area of a sector of angle 30° in a circle of radius 3.5 cm.

$$\Rightarrow A_{2} = \left\{ \frac{30}{360} \times \frac{22}{7} \times (3.5)^{2} \right\} cm^{2}$$

$$\Rightarrow A_{2} = \left\{ \frac{1}{12} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \right\} cm^{2} = \frac{77}{24} cm^{2}$$

$$\Rightarrow A_{2} = \left\{ \frac{1}{12} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \right\} cm^{2} = \frac{77}{24} cm^{2}$$

$$\therefore \quad \text{Area of the shaded region}$$

$$= A_{1} - A_{2} = \left(\frac{77}{6} - \frac{77}{24} \right) cm^{2}$$

$$= \frac{77}{24} \times (4 - 1) cm^{2} = 77/8 cm^{2} = 9.625 cm^{2}$$

$$\text{Given equation is}$$

$$\frac{1}{x + 4} - \frac{1}{x - 7} = \frac{11}{30}, x \neq -4, 7$$

$$\Rightarrow \frac{(x - 7) - (x + 4)}{(x + 4)(x - 7)} = \frac{11}{30}$$

$$\Rightarrow \frac{x - 7 - x - 4}{x^{2} - 7x + 4x - 28} = \frac{11}{30}$$

=

 $\Rightarrow \frac{-11}{x^2 - 3x - 28} = \frac{11}{30}$

 $\Rightarrow \frac{-1}{x^2 - 3x - 28} = \frac{1}{30}$

30.

 $x = \frac{-b \pm \sqrt{2^2 - 4ac}}{2a}$ $=\frac{-(-3)\pm\sqrt{(3)^2-4(1)(2)}}{2\times 1}$ (1) $=\frac{3\pm\sqrt{9-8}}{2}=\frac{3\pm\sqrt{1}}{2}=\frac{3\pm1}{2}$ \Rightarrow x = $\frac{3+1}{2}$ or x = $\frac{3-1}{2}$ x = $\frac{4}{2}$ or x = $\frac{2}{2}$ \therefore x = 2 or x = 1 Hence the roots of the given equation are 2 and 1.(1)0r Let $\frac{2x+3}{x-3} = y$...(i) Then, $\frac{x-3}{2x+3} = \frac{1}{x}$ (1/2) Therefore, the given equation reduces to $2y - 25\frac{1}{y} = 5$ $\Rightarrow 2y^2 - 25 = 5y$ $\Rightarrow 2y^2 - 5y - 25 = 0$ $\Rightarrow 2y^2 - 10y + 5y - 25 = 0$ [by factorisation method] $\Rightarrow 2y(y-5) + 5(y-5) = 0$ \Rightarrow (y - 5) (2y + 5) = 0 \Rightarrow y = 5 or y = $\frac{-5}{2}$ (1) Now, putting y = 5 in Eq. (i), we get $\frac{2x+3}{x-3} = \frac{5}{1}$ \Rightarrow 5x - 15 = 2x + 3 $\Rightarrow 3x = 18$ \Rightarrow x = 6 (1/2) Again, putting $y = \frac{5}{2}$ in Eq. (i), we get

 $\Rightarrow -30 = x^2 - 3x - 28$ $\Rightarrow x^2 - 3x + 2 = 0 (1)$

a = 1, b = -3 and c = 2

On comparing with the standard quadratic

equation $ax^2 + bx + c = 0$, we get

By using quadratic formula, we get



2x + 3 = 5x - 3 = 1 \Rightarrow 5x + 15 = 4x + 6 $\therefore 9x = 9$ $\Rightarrow x = 1$ Hence, the values of x are 1 and 6.(1)31. The given system of linear equations can be written as 2x + 3y - 7 = 0(a-b) x + (a+b) y - (3a+b-2) = 0The above system of equations is of the form $a_1x + b_1y + c_1 = 0$ $a_{2}x + b_{2}y + c_{2} = 0$, where $a_1 = 2, b_1 = 3, c_1 = -7$ $a_2 = (a - b), b_2 = (a + b), c_2 = -(3a + b)$ -2)For the given system of equations to have an infinite number of solutions $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ Here, $\frac{a_1}{a_2} = \frac{2}{a-b}$, $\frac{b_1}{b_2} = \frac{3}{a+b}$ and $\frac{c_1}{c_2} = \frac{-7}{-(3a+b-2)} = \frac{7}{3a+b-2}$ $\Rightarrow \frac{2}{a-b} = \frac{3}{a+b} = \frac{7}{3a+b-2}$ $\Rightarrow \frac{2}{a-b} = \frac{3}{a+b}$ and $\frac{3}{a+b} = \frac{7}{3a+b-2}$ \Rightarrow 2a + 2b = 3a - 3b and 9a + 3b - 6 = 7a + 7b \Rightarrow 2a - 3a = -3b - 2b and 9a - 7a = 7b -3b + 6 $\Rightarrow -a = -5b$ and 2a = 4b + 6 \Rightarrow a = 5b (3) and a = 2b + 3 (4) Solving (3) and (4) we get $5b = 2b + 3 \Longrightarrow b = 1$ Substituting b = 1 in (3), we get $a = 5 \times 1 = 5$ Thus, a = 5 and b = 1Hence, the given system of equations has infinite number of solutions when a = 5, b = 1

Let us assume, to the contrary, that $\sqrt{2}$ is rational. So, we can find integers r and s $(\neq 0)$ such that $\sqrt{2} = \frac{r}{s}$. Suppose r and s not having a common factor other than 1. Then, we divide by the common factor to get $\sqrt{2} = \frac{a}{k}$, where a and b are coprime. So, $b\sqrt{2} = a$. Squaring on both sides and rearranging, we get $2b^2 = a^2$. Therefore, 2 divides a^2 . Now, by Theorem it following that 2 divides a. So, we can write a = 2c for some integer c. Substituting for a, we get $2b^2 = 4c^2$, that $b^2 = 2c^2$. is. This means that 2 divides b^2 , and so 2 divides b (again using Theorem with p =2). Therefore, a and b have at least 2 as a common factor. But this contradicts the fact that a and b have no common factors other than 1. This contradiction has arisen because of our incorrect assumption that $\sqrt{2}$ is rational. So, we conclude that $\sqrt{2}$ is irrational. Or The number of participants in each room must be the HCF of 60, 84 and 108. (1) Now, prime factors of numbers 60, 84 and 108 are $60 = 2^2 \times 3 \times 5,$ $84 = 2^2 \times 3 \times 7$ and $108 = 2^2 \times 3^3$ HCF of (60, 84, 108) = $2^2 \times 3 = 12$ (2) Therefore, in each room maximum 12 participants can be seated, \therefore Total number of participants = 60 + 84+108 = 252

 \therefore Number of rooms required= $\frac{252}{12} = 21$ (2)

32.

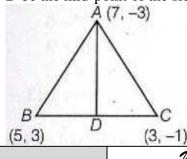
| below | 1 | |
|----------|-----------|-------------------------|
| Class | Frequency | Cumulative |
| interval | | frequency |
| 0-6 | 4 | 4 + 0 = 4 |
| 6-12 | Х | 4 + x = (4 + x) (c f) |
| 12-18 | 5(f) | 5 + (4 + x) = 9 + x |
| 18-24 | Y | y + (9 + x) = 9 + x + y |
| 24-30 | 1 | 1 + (9 + x + y) = |
| | | 10 + x + y |
| (1) | | |

33. Table for cumulative frequency is given below

(1)

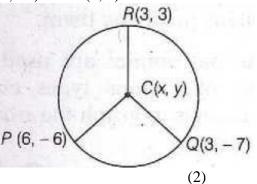
Since, N = 20 $\therefore 10 + x + y = 20$ \Rightarrow x + y = 20 - 10 \Rightarrow x + y = 10 ...(i) Also, we have, median = 14.4which lies in the class interval 12-18. (1) \therefore The median class is 12-18, such that l = 12, f = 5, c f = 4 + x and h = 6 $\therefore \text{ Median} = l + \left(\frac{\frac{N}{2} - cf}{f}\right) \times h$ $\Rightarrow 14.4 = 12 + \left| \frac{10 - (4 + x)}{5} \right| \times 6$ $\Rightarrow 14.4 - 12 = \frac{6-x}{5} \times 6$ $\Rightarrow 2.4 = \frac{36-6x}{5}$ $\Rightarrow 12 = 36 - 6x$ $\Rightarrow 6x = 24 \Rightarrow x = 4(1)$ Now, put the value of x in Eq. (i), we get $4 + y = 10 \Rightarrow y = 10 - 4 = 6$ Thus, x = 4 and y = 6(1)

34. The median from a vertex of a triangle bisects the opposite side, to that vertex. So, let AD be the median through A then D be the mid-point of the side BC.



Now, coordinates of $D = \left(\frac{5+3}{2}\frac{3-1}{2}\right) = (4,1)$ [\because coordinates of mid -point of line segment joining (x_1, y_1) and $(x_2, y_2) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$] and length of median AD is given by $AD = \sqrt{(x_2 - x_1)^2 + (y^2 + y_1)^2}$ [by distance formula] (1) $= \sqrt{(4-7)^2 + (1+3)^2} = \sqrt{(-3)^2 + (4)^2}$ $\sqrt{9+16} = \sqrt{25} = 5$ units (1) Also, OA = $\sqrt{(0-7)^2 + (0+3)^2}$ $= \sqrt{49+9} = \sqrt{58}$ units (1) *Or*

Let C (x, y) be the centre of the circle passing through the points P (6, - 6), Q (3, -7) and R (3, 3).



Then, PC = QC = CP [radii of circle] Now, PC = QC \Rightarrow PC² = QC² [squaring both sides] $\Rightarrow (x - 6)^2 + (y + 6)^2 = (x - 3)^2 + (y + 7)^2$ [\therefore distance = $\sqrt{(x_2 - x_1)^2 + (y^2 - y_1)^2}$] $\Rightarrow x^2 - 12.x + 36 + y^2 + 12y + 36$ $= x^2 - 6x + 9 + y^2 + 14y + 49$ [\therefore (a - b)² = a² + b² - 2ab] (1) $\Rightarrow -12x + 6x + 12y - 14y + 72 - 58 = 0$ $\Rightarrow -6x - 2y + 14 = 0$ $\Rightarrow 3x + y - 7 = 0$ [dividing by - 2] ...(i) and QC = CR \Rightarrow QC = CR [squaring both sides] $\Rightarrow (x - 3)^2 + (y + 7)^2 = (x - 3)^2 + (y - 3)^2$ $\Rightarrow (y + 7)^2 = (y - 3)^2 (1)$

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Page-7





$$\Rightarrow y^{2} + 14y + 49 = y^{2} - 6y + 9$$

$$\Rightarrow 20y + 40 = 0$$

$$\Rightarrow y = -\frac{40}{20} = -2 \dots (ii)$$

On putting $y = -2$ in Eq. (i), we get
 $3x - 2 - 7 = 0$

$$\Rightarrow 3x = 9$$

$$\Rightarrow x = 3$$

Hence, the centre of circle is (3,-2). (1)

35. Let BPC be the hemisphere and ABC be the cone standing on the base of the hemisphere (see figure). The radius BO of the hemisphere (as well as of the cone)

$$=\frac{1}{2}$$
 × 4 cm = 2 cm

So, volume of the toy = $\frac{2}{3}\pi r^3 + \frac{1}{3}\pi r^2 h$

$$\begin{bmatrix} \frac{2}{3} \times 3.14 \times (2)^3 + \frac{1}{3} \times 3.14 \times (2)^2 \times 2 \\ = 25.12 \text{ cm}^3 \end{bmatrix} \text{ cm}^3$$

Now, let the right circular cylinder EFGH circumscribe the given solid. The radius of the base of the right circular cylinder = HP = BO = 2 cm, and its height is EH = AO + OP = (2 + 2) cm = 4 cmSo, the volume required = Volume of the right circular cylinder volume of the toy $=(3.14 \times 2^{2} \times 4 - 25.12) \text{ cm}^{3}$ $= 25.12 \text{ cm}^3$ $= 25.12 \text{ cm}^3$ Hence, the required difference of the two volumes = 25.12 cm^3 . (i) Sol: -2 and 8 (ii) Zeroes are -2 and 8 $\therefore p(x) = k[x^2 - (\alpha + \beta)x + \alpha\beta]$ $= k[x^2 - (-2 + 8)x + (-2 \times 8)]$ $= k[x^2 - 6x - 16]$ But here parabola is inverted $\therefore p(x) = -(x^2 - 6x - 16)$

(iii)
$$p(x) = -x^2 + 3x - 2$$

 $p(x) = 0$
 $-x^2 + 3x - 2 = 0$
 $x^2 - 3x + 2 = 0$
 $x^2 - 2x - x + 2 = 0$

36.

$$x(x-2) - 1(x-2) = 0$$

(x-2) (x - 1) = 0
x = 2, x = 1

(iii)
$$(x-4)(x+7) = x^2 + 3x - 28$$

37. (i) To find the angle of elevation,
 $\tan \theta = \frac{\text{height of tower}}{\text{distance from tower}} = \frac{42}{42} = 1$
 $\theta = \tan^{-1}(1) = 45^{\circ}$
(ii) To find the distance,
 $\tan 60^{\circ} = \frac{\text{height of tower}}{\text{distance}} = \frac{42}{\text{distance}}$
 $\sqrt{3} = \frac{42}{\text{distance}}$
Distance $= \frac{42}{\sqrt{3}}$
Distance $= 24.24 \text{ m}$
(iii) To find the height of the verticle tower,
 $\tan 60^{\circ} = \frac{\text{height of the tower}}{\text{distance}}$
 $\sqrt{3} = \frac{\text{height of the tower}}{20}$
Height of the tower $= 20\sqrt{3}$
(iii) To find the angle of elevation of the sun,
 $\tan \theta = \frac{\text{height of the tower}}{\text{distance}}$
 $= \frac{1}{1}$ (since the ratios are in 1 : 1)
 $\theta = \tan^{-1}(1) = 45^{\circ}$
38. (i) $6\sqrt{3}$
(ii) 308 cm²
(iii) 1078 cm³
OR
(iii) 25 cm