

Ans. (1)

$$\text{Sol. } \sin x = \frac{-3}{5}, \pi < x < \frac{3\pi}{2}$$

$$\tan x = \frac{3}{4} \quad \cos x = -\frac{4}{5}$$

$$80(\tan^2 x - \cos x)$$

$$= 80 \left(\frac{9}{16} + \frac{4}{5} \right) = 45 + 64 = 109$$

- 12.** Let $I(x) = \int \frac{6}{\sin^2 x(1 - \cot x)^2} dx$. If $I(0) = 3$, then

$I\left(\frac{\pi}{12}\right)$ is equal to :

(1) $\sqrt{3}$ (2) $3\sqrt{3}$
(3) $6\sqrt{3}$ (4) $2\sqrt{3}$

Ans. (2)

$$\text{Sol. } I(x) = \int \frac{6dx}{\sin^2 x(1 - \cot x)^2} = \int \frac{6 \csc^2 x dx}{(1 - \cot x)^2}$$

$$\text{Put } 1 - \cot x = t$$

$$\cosec^2 x \, dx = dt$$

$$I = \int \frac{6dt}{t^2} = \frac{-6}{t} + C$$

$$I(x) = \frac{-6}{1 - \cot x} c, c = 3$$

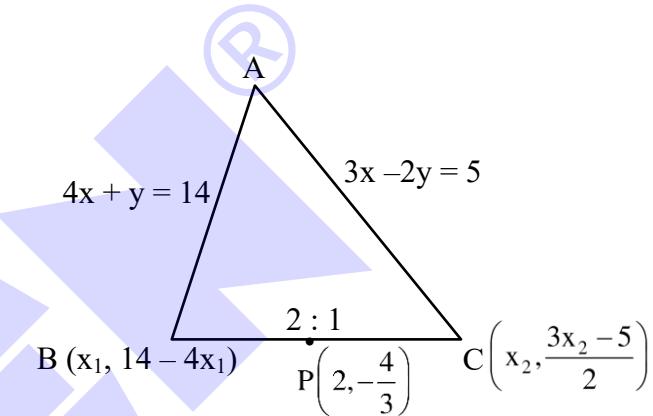
$$I(x) = 3 - \frac{6}{1 - \cot x}, \quad I\left(\frac{\pi}{12}\right) = 3 - \frac{6}{1 - (2 + \sqrt{3})}$$

$$I\left(\frac{\pi}{12}\right) = 3 + \frac{6}{\sqrt{3}+1} = 3 + \frac{6(\sqrt{3}-1)}{2} = 3\sqrt{3}\sqrt{2}$$

13. The equations of two sides AB and AC of a triangle ABC are $4x + y = 14$ and $3x - 2y = 5$, respectively. The point $\left(2, -\frac{4}{3}\right)$ divides the third side BC internally in the ratio 2 : 1. The equation of the side BC is :

(1) $x - 6y - 10 = 0$ (2) $x - 3y - 6 = 0$
 (3) $x + 3y + 2 = 0$ (4) $x + 6y + 6 = 0$

Sol.



$$\frac{2x_2 + x_1}{3} = 2, \quad \frac{\frac{2(3x_2 - 5)}{2} + (14 - 4x_1)}{3} = \frac{-4}{3}$$

$$2x_2 + x_1 = 6, \quad 3x_2 - 4x_1 = -13$$

$$x_2 = 1, x_1 = 4$$

So, C(1, -1), B(4, -2)

$$m = \frac{-1}{3}$$

$$\text{Equation of BC : } y + 1 = \frac{-1}{3}(x - 1)$$

$$3y + 3 = -x + 1$$

$$x + 3y + 2 = 0$$



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17. For the function $f(x) = (\cos x) - x + 1$, $x \in \mathbb{R}$, between the following two statements
(S1) $f(x) = 0$ for only one value of x is $[0, \pi]$.
(S2) $f(x)$ is decreasing in $\left[0, \frac{\pi}{2}\right]$ and increasing in $\left[\frac{\pi}{2}, \pi\right]$.

(1) Both (S1) and (S2) are correct

(2) Only (S1) is correct

(3) Both (S1) and (S2) are incorrect

(4) Only (S2) is correct

Ans. (2)

Sol. $f(x) = \cos x - x + 1$

$$f(x) = -\sin x - 1$$

f is decreasing $\forall x \in \mathbb{R}$

$$f(x) = 0$$

$$f(0) = 2, f(\pi) = -\pi$$

f is strictly decreasing in $[0, \pi]$ and $f(0).f(\pi) < 0$

\Rightarrow only one solution of $f(x) = 0$

S1 is correct and S2 is incorrect.

18. The set of all α , for which the vector $\vec{a} = \alpha \hat{i} + 6\hat{j} - 3\hat{k}$ and $\vec{b} = \hat{t}\hat{i} - 2\hat{j} - 2\alpha\hat{k}$ are inclined at an obtuse angle for all $t \in \mathbb{R}$ is :

(1) $[0, 1)$

(2) $(-2, 0]$

(3) $\left(-\frac{4}{3}, 0\right]$

(4) $\left(-\frac{4}{3}, 1\right)$

Ans. (3)

Sol. $\vec{a} = \alpha \hat{i} + 6\hat{j} - 3\hat{k}$

$$\vec{b} = \hat{t}\hat{i} - 2\hat{j} - 2\alpha\hat{k}$$

so $\vec{a} \cdot \vec{b} < 0$, $\forall t \in \mathbb{R}$

$$\alpha t^2 - 12 + 6\alpha t < 0$$

$$\alpha t^2 + 6\alpha t - 12 < 0, \forall t \in \mathbb{R}$$

$\alpha < 0$, and D < 0

$$36\alpha^2 + 48\alpha < 0$$

$$12\alpha(3\alpha + 4) < 0$$

$$\frac{-4}{3} < \alpha < 0$$

also for $a = 0$, $\vec{a} \cdot \vec{b} < 0$

hence $a \in \left(-\frac{4}{3}, 0\right]$

19. Let $y = y(x)$ be the solution of the differential equation $(1 + y^2)e^{\tan x}dx + \cos^2 x(1 + e^{2\tan x})dy = 0$, $y(0) = 1$. Then $y\left(\frac{\pi}{4}\right)$ is equal to :

(1) $\frac{2}{e}$

(2) $\frac{1}{e^2}$

(3) $\frac{1}{e}$

(4) $\frac{2}{e^2}$

Ans. (3)

Sol. $(1 + y^2)e^{\tan x}dx + \cos^2 x(1 + e^{2\tan x})dy = 0$

$$\int \frac{\sec^2 x e^{\tan x}}{1 + e^{2\tan x}} dx + \int \frac{dy}{1 + y^2} = C$$

$$\Rightarrow \tan^{-1}(e^{\tan x}) + \tan^{-1} y = C$$

$$\text{for } x = 0, y = 1, \tan^{-1}(1) + \tan^{-1} 1 = C$$

$$C = \frac{\pi}{2}$$

$$\tan^{-1}(e^{\tan x}) + \tan^{-1} y = \frac{\pi}{2}$$

$$\text{Put } x = \pi, \tan^{-1} e + \tan^{-1} y = \frac{\pi}{2}$$

$$\tan^{-1} y = \cot^{-1} e$$

$$y = \frac{1}{e}$$

20. Let $H : \frac{-x^2}{a^2} + \frac{y^2}{b^2} = 1$ be the hyperbola, whose eccentricity is $\sqrt{3}$ and the length of the latus rectum is $4\sqrt{3}$. Suppose the point $(\alpha, 6)$, $\alpha > 0$ lies on H . If β is the product of the focal distances of the point $(\alpha, 6)$, then $\alpha^2 + \beta$ is equal to :

(1) 170

(2) 171

(3) 169

(4) 172

Ans. (2)



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Sol. $H : \frac{y^2}{b^2} - \frac{x^2}{a^2} = 1, e = \sqrt{3}$

$$e = \sqrt{1 + \frac{a^2}{b^2}} = \sqrt{3} \Rightarrow \frac{a^2}{b^2} = 2$$

$$a^2 = 2b^2$$

$$\text{length of L.R.} = \frac{2a^2}{b} = 4\sqrt{3}$$

$$a = \sqrt{6}$$

$$P(\alpha, 6) \text{ lie on } \frac{y^2}{3} - \frac{x^2}{6} = 1$$

$$12 - \frac{\alpha^2}{6} = 1 \Rightarrow \alpha^2 = 66$$

$$\text{Foci} = (0, \pm be) = (0, 3) \& (0, -3)$$

Let d_1 & d_2 be focal distances of $P(\alpha, 6)$

$$d_1 = \sqrt{\alpha^2 + (6+be)^2}, d_2 = \sqrt{\alpha^2 + (6-be)^2}$$

$$d_1 = \sqrt{66+81}, d_2 = \sqrt{66+9}$$

$$\beta = d_1 d_2 = \sqrt{147 \times 75} = 105$$

$$\alpha^2 + \beta = 66 + 105 = 171$$

SECTION-B

21. Let $A = \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix}$. If the sum of the diagonal elements of A^{13} is 3^n , then n is equal to _____.

Ans. (7)

Sol. $A = \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix}$

$$A^2 = \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 3 & -3 \\ 3 & 0 \end{bmatrix}$$

$$A^3 = \begin{bmatrix} 3 & -3 \\ 3 & 0 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 3 & -6 \\ 6 & -3 \end{bmatrix}$$

$$A^4 = \begin{bmatrix} 3 & -6 \\ 6 & -3 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 0 & -9 \\ 9 & -9 \end{bmatrix}$$

$$A^5 = \begin{bmatrix} 0 & -9 \\ 9 & -9 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} -9 & -9 \\ 9 & -18 \end{bmatrix}$$

$$A^6 = \begin{bmatrix} -9 & -9 \\ 9 & -18 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} -27 & 0 \\ 0 & -27 \end{bmatrix}$$

$$A^7 = \begin{bmatrix} -27 & 0 \\ 0 & -27 \end{bmatrix} \begin{bmatrix} -54 & 27 \\ -27 & -27 \end{bmatrix} = \begin{bmatrix} 3^6 \times 2 & -27^2 \\ 27^2 & 3^6 \end{bmatrix}$$

$$3^7 = 3^n \Rightarrow n = 7$$

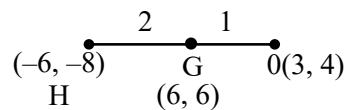
22. If the orthocentre of the triangle formed by the lines $2x + 3y - 1 = 0$, $x + 2y - 1 = 0$ and $ax + by - 1 = 0$, is the centroid of another triangle, whose circumcentre and orthocentre respectively are $(3, 4)$ and $(-6, -8)$, then the value of $|a - b|$ is _____.

Ans. (16)

Sol. $2x + 3y - 1 = 0$

$$x + 2y - 1 = 0$$

$$ax + by - 1 = 0$$



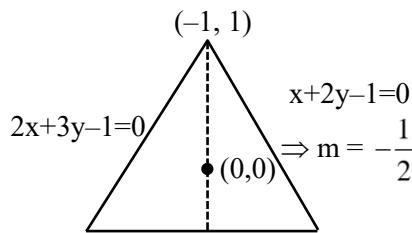
$$\left(\frac{6-6}{3}, \frac{8-8}{3} \right)$$

$$= (0, 0)$$



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$$ax + by - 1 = 0$$

$$\left(\frac{1-0}{-1-0} \right) \left(\frac{-a}{b} \right) = -1$$

$$\Rightarrow -a = b$$

$$\Rightarrow ax - ay - 1 = 0$$

$$ax - a\left(1 - \frac{2x}{3}\right) - 1$$

$$x\left(a + \frac{2a}{3}\right) = \frac{a}{3}$$

$$x = \frac{a+3}{5a}$$

$$2\left(\frac{a+3}{5a}\right) + 3y - 1 = 0$$

$$y = \frac{1 - \frac{2a+6}{5a}}{3} = \frac{3a-6}{3 \times 5a}$$

$$y = \frac{a-2}{5a}$$

$$\frac{\left(\frac{a-2}{5a}\right)}{\left(\frac{a+3}{5a}\right)} = 2 \Rightarrow a-2 = 2a+6$$

$$a = -8$$

$$b = 8$$

$$-8x + 8y - 1 = 0$$

$$|a - b| = 16$$

23. Three balls are drawn at random from a bag containing 5 blue and 4 yellow balls. Let the random variables X and Y respectively denote the number of blue and Yellow balls. If \bar{X} and \bar{Y} are the means of X and Y respectively, then $7\bar{X} + 4\bar{Y}$ is equal to _____.

Ans. (17)

Sol.

Blue balls	0	1	2	3	4	5
Prob.	$\frac{{}^5C_0 \cdot {}^4C_1}{{}^9C_3}$	$\frac{{}^5C_1 \cdot {}^4C_2}{{}^9C_3}$	$\frac{{}^5C_2 \cdot {}^4C_1}{{}^9C_3}$	$\frac{{}^5C_3 \cdot {}^4C_0}{{}^9C_3}$	0	0

$$7\bar{X} = \frac{{}^5C_1 \cdot {}^4C_2 + {}^5C_2 \cdot {}^4C_1 \times 2 + {}^5C_3 \cdot {}^4C_0 \times 3}{{}^9C_3} \times 7$$

$$\begin{aligned} & \frac{30 + 80 + 30}{84} \times 7 \\ &= \frac{140}{12} = \frac{70}{6} = \frac{35}{3} \end{aligned}$$

yellow	0	1	2	3	4
	${}^5C_2 \cdot {}^4C_1$	${}^5C_1 \cdot {}^4C_2$	${}^5C_0 \cdot {}^4C_3$	0	

$$4\bar{Y} = \frac{40 + 60 + 12}{84} \times 4 = \frac{112}{21} = \frac{16}{3}$$

24. The number of 3-digit numbers, formed using the digits 2, 3, 4, 5 and 7, when the repetition of digits is not allowed, and which are not divisible by 3, is equal to _____.

Ans. (36)

Sol. 2, 3, 4, 5, 7

total number of three digit numbers not divisible by 3 will be formed by using the digits

(4, 5, 7)

(3, 4, 7)

(2, 5, 7)

(2, 4, 7)

(2, 4, 5)

(2, 3, 5)

number of ways = $6 \times 3! = 36$



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25. Let the positive integers be written in the form :

	1	
2	3	
4	5	6
7	8	9
.	10	.

If the k^{th} row contains exactly k numbers for every natural number k , then the row in which the number 5310 will be, is _____.

Ans. (103)

Sol. $S = 1 + 2 + 4 + 7 + \dots + T_n$

$$S = 1 + 2 + 4 + \dots$$

$$T_n = 1 + 1 + 2 + 3 + \dots + (T_{n-1} - T_{n-1})$$

$$T_n = 1 + \left(\frac{n-1}{2} \right) [2 + (n-2) \times 1]$$

$$T_n = 1 + 1 + \frac{n(n-1)}{2}$$

$$n = 100 \quad T_n = 1 + \frac{100 \times 99}{2} = 4950 + 1$$

$$n = 101 \quad T_n = 1 + \frac{101 \times 100}{2} = 5050 + 1 = 5051$$

$$n = 102 \quad T_n = 1 + \frac{102 \times 101}{2} = 5151 + 1 = 5152$$

$$n = 103 \quad T_n = 1 + \frac{103 \times 102}{2} = 5254$$

$$n = 104 \quad T_n = 1 + \frac{104 \times 103}{2} = 5357$$

26. If the range of $f(\theta) = \frac{\sin^4 \theta + 3\cos^2 \theta}{\sin^4 \theta + \cos^2 \theta}$, $\theta \in \mathbb{R}$ is $[\alpha, \beta]$, then the sum of the infinite G.P., whose first term is 64 and the common ratio is $\frac{\alpha}{\beta}$, is equal to _____.

Ans. (96)

Sol. $f(\theta) = \frac{\sin^4 \theta + 3\cos^2 \theta}{\sin^4 \theta + \cos^2 \theta}$

$$f(\theta) = 1 + \frac{2\cos^2 \theta}{\sin^4 \theta + \cos^2 \theta}$$

$$f(\theta) = \frac{2\cos^2 \theta}{\cos^4 \theta - \cos^2 \theta + 1} + 1$$

$$f(\theta) = \frac{2}{\cos^2 \theta + \sec^2 \theta - 1} + 1$$

$$f(\theta)|_{\min.} = 1$$

$$f(\theta)_{\max.} = 3$$

$$S = \frac{64}{1 - 1/3} = 96$$

27. Let $\alpha = \sum_{r=0}^n (4r^2 + 2r + 1)^n C_r$

$$\text{and } \beta = \left(\sum_{r=0}^n \frac{n C_r}{r+1} \right) + \frac{1}{n+1}. \text{ If } 140 < \frac{2\alpha}{\beta} < 281,$$

then the value of n is _____.

Ans. (5)

Sol. $\alpha = \sum_{r=0}^n (4r^2 + 2r + 1)^n C_r$

$$\alpha = 4 \sum_{r=0}^n r^2 \cdot \frac{n}{r} \cdot {}^{n-1} C_{r-1} + 2 \sum_{r=0}^n r \cdot \frac{n}{r} \cdot {}^{n-1} C_{r-1} + \sum_{r=0}^n {}^n C_r$$

$$+ 4n \sum_{r=0}^n {}^{n-1} C_{r-1} + 2n \sum_{r=0}^n {}^{n-1} C_{r-1} + \sum_{r=0}^n {}^n C_r$$

$$\alpha = 4n(n-1) \cdot 2^{n-2} + 4n \cdot 2^{n-1} + 2n \cdot 2^{n-1} + 2^n$$

$$\alpha = 2^{n-2} [4n(n-1) + 8n + 4n + 4]$$

$$\alpha = 2^{n-2} [4n^2 + 8n + 4]$$

$$\alpha = 2n(n+1)^2$$

$$\beta = \sum_{r=0}^n \frac{{}^n C_r}{r+1} + \frac{1}{n+1}$$

$$= \sum_{r=0}^n \frac{{}^{n+1} C_{r+1}}{n+1} + \frac{1}{n+1}$$

$$= \frac{1}{n+1} (1 + {}^{n+1} C_1 + \dots + {}^{n+1} C_{n+1})$$

$$= \frac{2^{n+1}}{n+1}$$

$$\frac{2\alpha}{\beta} = \frac{2^{n+1}(n+1)^2}{2^{n+1}} \cdot (n+1) = (n+1)^3$$

$$140 < (n+1)^3 < 281$$

$$n = 4 \Rightarrow (n+1)^3 = 125$$

$$n = 5 \Rightarrow (n+1)^3 = 216$$

$$n = 6 \Rightarrow (n+1)^3 = 343$$

$$\therefore n = 5$$



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28. Let $\vec{a} = 9\hat{i} - 13\hat{j} + 25\hat{k}$, $\vec{b} = 3\hat{i} + 7\hat{j} - 13\hat{k}$ and $\vec{c} = 17\hat{i} - 2\hat{j} + \hat{k}$ be three given vectors. If \vec{r} is a vector such that $\vec{r} \times \vec{a} = (\vec{b} + \vec{c}) \times \vec{a}$ and $\vec{r} \cdot (\vec{b} - \vec{c}) = 0$, then $\frac{|593\vec{r} + 67\vec{a}|^2}{(593)^2}$ is equal to _____.

Ans. (569)

Sol. $\vec{a} = 9\hat{i} - 13\hat{j} + 25\hat{k}$

$$\vec{b} = 3\hat{i} + 7\hat{j} - 13\hat{k}$$

$$\vec{c} = 17\hat{i} - 2\hat{j} + \hat{k}$$

$$\vec{b} + \vec{c} = 20\hat{i} + 5\hat{j} - 12\hat{k}$$

$$\vec{b} - \vec{c} = -14\hat{i} + 9\hat{j} - 14\hat{k}$$

$$(\vec{r} - (\vec{b} + \vec{c})) \times \vec{a} = 0$$

$$\vec{r} - (\vec{b} + \vec{c}) = \lambda \vec{a}$$

$$\vec{r} = \lambda \vec{a} + \vec{b} + \vec{c}$$

But $\vec{r} \cdot (\vec{b} - \vec{c}) = 0$

$$\Rightarrow (\lambda \vec{a} + \vec{b} + \vec{c}) \cdot (\vec{b} - \vec{c}) = 0$$

$$\Rightarrow \lambda \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{b} + \vec{c} \cdot \vec{b} - \lambda \vec{a} \cdot \vec{c} - \vec{b} \cdot \vec{c} - \vec{c} \cdot \vec{c} = 0$$

$$\lambda = \frac{\vec{c} \cdot \vec{c} - \vec{b} \cdot \vec{b}}{\vec{a} \cdot \vec{b} - \vec{a} \cdot \vec{c}} = \frac{294 - 227}{-389 + 204} = \frac{-67}{593}$$

$$\therefore \vec{r} = \vec{b} + \vec{c} - \frac{67}{593} \vec{a}$$

$$\Rightarrow 593\vec{r} + 67\vec{a} = 593(\vec{b} + \vec{c})$$

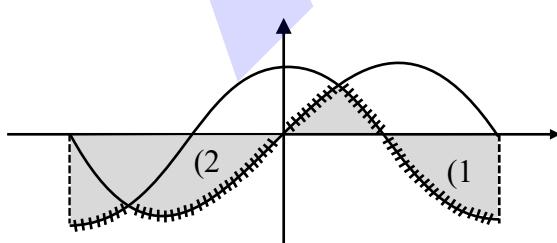
$$\Rightarrow |\vec{b} + \vec{c}|^2 = 569$$

29. Let the area of the region enclosed by the curve $y = \min\{\sin x, \cos x\}$ and the x-axis between $x = -\pi$ to $x = \pi$ be A. Then A^2 is equal to _____.

Ans. (16)

Sol. $y = \min\{\sin x, \cos x\}$

x-axis $x = -\pi$ $x = \pi$



$$\int_0^{\pi/4} \sin x = (\cos x)_{\pi/4}^0 = 1 - \frac{1}{\sqrt{2}}$$

$$\int_{-\pi}^{-3\pi/4} (\sin x - \cos x) = (-\cos x - \sin x)_{-\pi}^{-3\pi/4}$$

$$= (\cos x + \sin x)_{-3\pi/4}^{-\pi}$$

$$= (-1 + 0) - \left(-\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} \right)$$

$$= -1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}$$

$$\int_{\pi/4}^{\pi/2} \cos x dx = (\sin x)_{\pi/4}^{\pi/2} = 1 - \frac{1}{\sqrt{2}}$$

$$A = 4$$

$$A^2 = 16$$

30. The value of

$$\lim_{x \rightarrow 0} 2 \left(\frac{1 - \cos x \sqrt{\cos 2x} \sqrt[3]{\cos 3x} \dots \sqrt[10]{\cos 10x}}{x^2} \right) \text{ is } \underline{\hspace{2cm}}$$

Ans. (55)

Sol.

$$\lim_{x \rightarrow 0} 2 \left(\frac{1 - \left(1 - \frac{x^2}{2!}\right) \left(1 - \frac{4x^2}{2!}\right) \left(1 - \frac{9x^2}{2!}\right) \dots \left(1 - \frac{100x^2}{2!}\right)}{x^2} \right)$$

By expansion

$$\lim_{x \rightarrow 0} \frac{2 \left(1 - \left(1 - \frac{x^2}{2}\right) \left(1 - \frac{1}{2} \cdot \frac{4x^2}{2}\right) \left(1 - \frac{1}{3} \cdot \frac{9x^2}{2}\right) \dots \left(1 - \frac{1}{10} \cdot \frac{100x^2}{2}\right) \right)}{x^2}$$

$$\lim_{x \rightarrow 0} 2 \left(\frac{1 - \left(1 - \frac{x^2}{2}\right) \left(1 - \frac{2x^2}{2}\right) \left(1 - \frac{3x^2}{2}\right) \dots \left(1 - \frac{10x^2}{2}\right)}{x^2} \right)$$

$$\lim_{x \rightarrow 0} \frac{2 \left(1 - 1 + x^2 \left(\frac{1}{2} + \frac{2}{2} + \frac{3}{2} + \dots + \frac{10}{2} \right) \right)}{x^2}$$

$$2 \left(\frac{1}{2} + \frac{2}{2} + \frac{3}{2} + \dots + \frac{10}{2} \right)$$

$$1 + 2 + \dots + 10 = \frac{10 \times 11}{2} = 55$$



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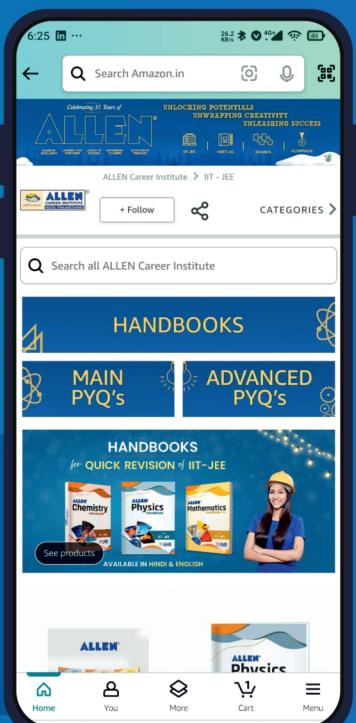
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